

MJC/2011/P1/10(a)

State a sequence of transformations which transform the graph of $x^2 + y^2 = 1$ to the graph of

$$(x-1)^2 + y^2 = 4.$$

[3]

10	Curve Sketching and Transformations of Graphs
(a)	$x^2 + y^2 = 1$ <p style="text-align: right;">↓ Replace x by $\frac{x}{2}$</p> $\left(\frac{x}{2}\right)^2 + y^2 = 1$ <p style="text-align: right;">↓ Replace x by $x-1$</p> $\left(\frac{x-1}{2}\right)^2 + y^2 = 1$ <p style="text-align: right;">↓ Replace y by $\frac{y}{2}$</p> $\left(\frac{x-1}{2}\right)^2 + \left(\frac{y}{2}\right)^2 = 1$ $\Rightarrow (x-1)^2 + y^2 = 4$ <p>The transformations are scaling parallel to x-axis with a scale factor 2, followed by a translation of 1 units in the direction of x-axis and scaling parallel to y-axis with a scale factor 2.</p> <p>Alternative Solution</p> $x^2 + y^2 = 1$ <p style="text-align: right;">↓ Replace x by $x - \frac{1}{2}$</p> $\left(x - \frac{1}{2}\right)^2 + y^2 = 1$ <p style="text-align: right;">↓ Replace x by $\frac{x}{2}$</p> $\left(\frac{x}{2} - \frac{1}{2}\right)^2 + y^2 = 1$ <p style="text-align: right;">↓ Replace y by $\frac{y}{2}$</p>

$$\left(\frac{x-1}{2}\right)^2 + \left(\frac{y}{2}\right)^2 = 1$$
$$\Rightarrow (x-1)^2 + y^2 = 4$$

The transformations are translation of $\frac{1}{2}$ units in the direction of x -axis, followed by scaling parallel to x -axis with a scale factor 2 and scaling parallel to y -axis with a scale factor 2.

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